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Model-based Reconstruction with Automatic Scaling for Real-Time Phase-Contrast Flow MRI with Complementary Sets of Radial Spokes

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Synopsis

Real-time phase-contrast flow MRI is extended from sequential acquisitions of flow-compensated and flow-encoded data with the same set of radial spokes to interleaved acquisitions with different radial spokes oriented by a small Golden angle, thereby improving spatial accuracy and reducing streaking artifacts. To apply model-based reconstructions for this sampling scheme, an automatic scaling of unknowns is proposed, which is capable of balancing partial derivatives and regularizations during the iterative nonlinear inversion.

Purpose

To develop a model-based reconstruction technique with automatic scaling of unknowns for real-time phase-contrast flow MRI acquired via highly undersampled radial FLASH with complementary spokes for flow-compensated and flow-encoded data.

Methods

In current real-time phase-contrast flow MRI, both the flow-compensated and flow-encoded data are sequentially acquired via radial spokes with the same k-space encoding^{1,2}. In the model-based reconstruction³, the forward model is formulated as $F_{j,l}(x) = U_l \mathcal{F}\{\rho \cdot e^{i\Delta\phi \cdot S_l} \cdot c_j\}$, where the vector $x = (\rho, \Delta\phi, c_1, \dots, c_N)^T$ of unknowns comprises ρ the proton density, $\Delta\phi$ the phase difference (i.e. velocity), c_j the j th coil sensitivity map, and U_l the sampling pattern of the l th acquisition. The velocity-encoding (Venc) indices $S_1 = 0$ and $S_2 = 1$ represent the flow-compensated and flow-encoded acquisition, respectively. The unknowns in this nonlinear signal model are solved by the iteratively regularized Gauss-Newton method with Tikhonov regularization on all unknowns. The balance of partial derivatives and regularizations is achieved by scaling of Venc indices:

$\hat{S}_l = \frac{\|M\|_2}{\|\Delta\phi\|_2} \cdot S_l$, where M and $\Delta\phi$ are approximated by the mean and complex difference of the gridded multi-channel k-space data from the flow-compensated and flow-encoded acquisition, respectively.

Here, we modify the pulse sequence to allow for complementary sets of spokes. As shown in Figure 1, each pair of flow-compensated and flow-encoded spokes is sampled in an interleaved manner and separated by a constant Golden angle⁴ of 27.19840° , which is chosen such that the two sets of spokes for one velocity map lead to a nearly uniform coverage of k-space. First, compared to the current sampling scheme^{1,2}, the proposed scheme samples twice more different spokes, thereby effectively reducing the undersampling factor. Second, this sampling scheme enables an additional sliding window reconstruction, which can further increase the frame rate. The main drawback of this sampling scheme, however, is the incompatibility with the previous scaling³, which requires the calculation of the complex difference. As shown in Figure 2, the complex difference between the gridded flow-compensated and flow-encoded k-space sampled with same spokes emphasizes only the flow region (i.e. aorta), while the complex difference from complementary spokes suffers from severe streaks surrounding not only the flow region but also the "static" region (i.e. chest wall). Consequently, the redundant streaks contribute false-positive information to the scaling calculation.

To allow for complementary sets of radial spokes, the model-based reconstruction requires automatic scaling of unknowns, which seeks for the appropriate scaling during iterative reconstructions⁵. In principle, the scaling of the m th unknown reads as $\hat{x}^{(m)} = x^{(m)} \cdot \gamma_m$, where γ_m is chosen such that sensitivities of the data with respect to different solution components are balanced, so $\gamma_m = \|DF(x)|_{x^{(m)}}\| = \|DF(x)P_m^H\|$ with $DF(x)$ the derivative of the forward operator and P_m^H the projection onto the m th unknown. The spectral radius of this matrix norm is determined by its maximal eigenvalue⁶: $\gamma_m = \lambda_0(P_m DF^H(x)DF(x)P_m^H)^{1/2}$, approximated by the power method. In the current implementation, the power method with 10 iterations is used only for the odd Newton iterations of each frame.

Experimental implementations of real-time phase-contrast flow MRI use undersampled radial FLASH with the Golden-angle interleaved acquisition scheme. All measurements (TE = 1.70 ms, flip angle 10°) had 1.5 mm in-plane resolution, 320 mm field-of-view, 6 mm slice thickness, and 35.7 ms (7 spokes, TR = 2.55 ms) temporal resolution corresponding to 28 frames per second.

Results & Discussion

As shown in Figure 3, the automatically scaled model-based reconstruction of complementary sets of spokes yields magnitude images with clearer delineations of small vessels, increased sharpness, and reduced streaking artifacts compared to reconstructions from same sets of spokes. The corresponding phase-contrast velocity maps from complementary sets of spokes tend to be smoother than those from same spokes. Quantitative evaluations of mean velocities spatially averaged over the lumen of the ascending aorta are provided in Figure 4 for both same spokes and complementary spokes. While systolic peak velocities are similar for both acquisition schemes, low velocities during diastole from complementary spokes exhibit more fluctuations than from same spokes.

Conclusion

The proposed automatically scaled model-based reconstruction for real-time phase-contrast flow MRI allows for accurate estimates of flow velocities for two different acquisition schemes: same sets of radial spokes and complementary sets of Golden-angle radial spokes for flow-compensated and flow-encoded acquisitions. While velocity maps are of similar quality, complementary spokes substantially improve the spatial accuracy of magnitude images.

Acknowledgements

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References

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Figures

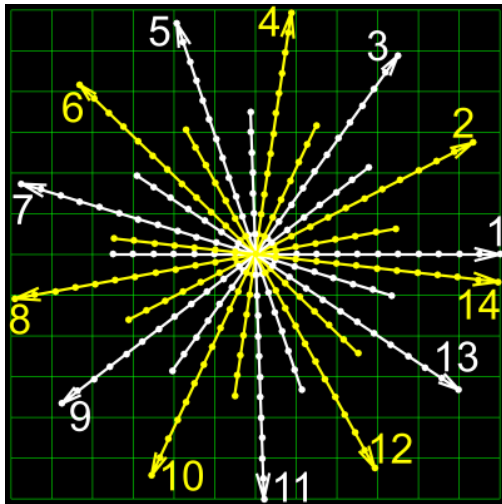


Figure 1. An interleaved acquisition scheme with the small Golden angle of 27.19840° for the (white) flow-compensated and the (yellow) flow-encoded data. This Golden angle is chosen such that the total of 2×7 radial spokes covers the view angle of 360° . The numbers indicate the acquisition orders of radial spokes with the asymmetry of 30 %.

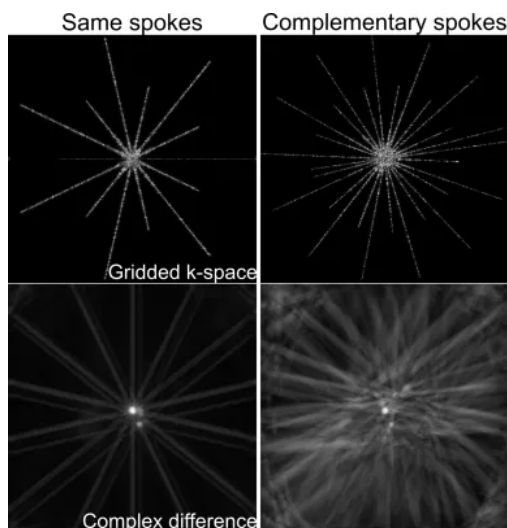


Figure 2. A representative systolic (bottom) complex-difference image of (top) gridded flow-compensated and flow-encoded data, acquired by (left) same spokes with turn-based sequential scheme and (right) complementary spokes with Golden-angle interleaved scheme, respectively.

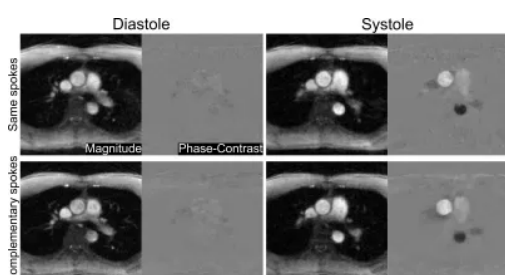


Figure 3. Representative (left) diastolic and (right) systolic magnitude and phase-contrast velocity maps via the proposed automatically scaled model-based reconstructions of (top) same sets of spokes and (bottom) complementary sets of spokes, respectively.

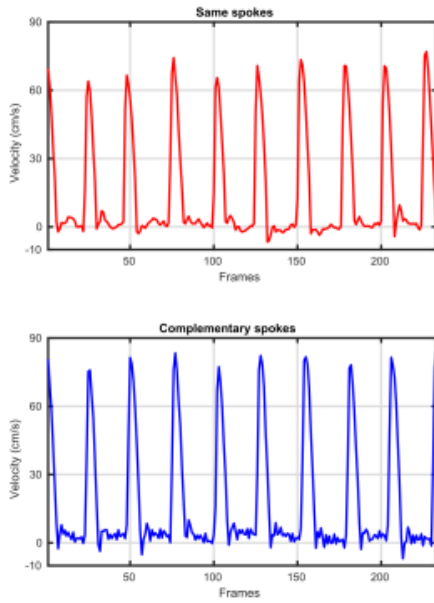


Figure 4. Mean flow velocities spatially averaged over the lumen of the ascending aorta as obtained by (top) same sets of spokes and (bottom) complementary sets of spokes, respectively.